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RESEARCH ARTICLE

PERFORMANCE ANALYSIS OF IMAGE COMPRESSION USING DCT AND DWT

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Abstract— Image compression is a key technology in transmission and storage of digital images because of vast data associated with them. This research suggests a new image compression scheme with pruning proposal based on discrete wavelet transformation (DWT). The effectiveness of the algorithm has been justified over some real images, and the performance of the algorithm has been compared with other common compression standards. Experimental results demonstrate that the proposed technique provides sufficient high compression ratios compared to other compression techniques.

Keywords-“Discrete cosine transform (DCT)”, “Discrete wavelet transform (DWT)”

I. INTRODUCTION

Image compression is important for many applications that involve huge data storage, transmission and retrieval such as for multimedia, documents, videoconferencing, and medical imaging. Uncompressed images require considerable storage capacity and transmission bandwidth. The objective of image compression technique is to reduce redundancy of the image data in order to be able to store or transmit data in an efficient form. This results in the reduction of file size and allows more images to be stored in a given amount of disk or memory space.

Image compression can be lossy or lossless. In a lossless compression algorithm, compressed data can be used to recreate an exact replica of the original; no information is lost to the compression process. This type of compression is also known as entropy coding. This name comes from the fact that a compressed signal is generally more random than the original; patterns are removed when a signal is compressed. While lossless compression is useful for exact reconstruction, it generally does not provide sufficiently high compression ratios to be truly useful in image compression.

In lossy compression, the original signal cannot be exactly reconstructed from the compressed data. The reason is that, much of the detail in an image can be discarded without greatly changing the appearance of the image. As an example consider an image of a tree, which occupies several hundred megabytes. In lossy image compression, though very fine details of the images are lost, but image size is drastically reduced. Lossy image compressions are useful in applications such as broadcast television, videoconferencing, and facsimile

transmission, in which a certain amount of error is an acceptable trade-off for increased compression performance. Methods for lossy compression include: Fractal compression, Transform coding, Fourier-related transform, DCT (Discrete Cosine Transform) and Wavelet transform.

II. RELATED WORK

DISCRETE COSINE TRANSFORM (DCT)

Data compression ratio, also known as compression power, is used to quantify the reduction in data-representation size produced by data compression. The data compression ratio is analogous to the physical compression ratio it is used to measure physical compression of substances, and is defined in the same way, as the ratio between the uncompressed size and the compressed size.

DCT is used because next reasons:

1. For high correlated data, the compression rate obtained by DCT is getting close to that obtained using the optimum Karhunen – Loeve transform.
2. DCT is an orthogonal transform. So, if in a matrix form, the DCT output is $Y=TXT^t$, then the inverse transform is $X=T^tYT$. The $X \rightarrow Y$ is named the direct DCT, and is given by,

$$Y_{kl} = \frac{c_k c_l}{4} \sum_{i=0}^7 \sum_{j=0}^7 x_{ij} \cos\left(\frac{(2i+1)k\pi}{16}\right) \cos\left(\frac{(2j+1)l\pi}{16}\right) \tag{2.1}$$

where $k, l=0, \dots, 7$ & $c_k = \begin{cases} 1 & k = 0 \\ \sqrt{2} & k = 1, \dots, 7 \end{cases}$

DCT can be written in matrix form, as $y=Tx$, where $x=\{x_{00}, \dots, x_{07}, x_{10}, \dots, x_{17}, \dots, x_{77}\}$, and T is a matrix, whose elements are the products of the cosine functions defined before.

The inverse DCT transform can be written as:

$$x_{ij} = \frac{\sum_{k=0}^7 \sum_{l=0}^7 y_{kl} c_k c_l}{4} \cos\left(\frac{(2i+1)k\pi}{16}\right) \cos\left(\frac{(2j+1)l\pi}{16}\right) \tag{2.2}$$

An important feature of 2-D DCT and of 2-D IDCT is separability. This means these 2 bidimensional transforms, written in matrix form, can be computed by performing 1-D DCT first on the rows, then on the columns of this matrix.

The 1-D DCT is:

$$z_{k=\frac{c(k)}{2}} = \sum_{l=0}^7 x_l \cos\left(\frac{(2l+1)k\pi}{16}\right) \tag{2.3}$$

This equation can be written in matrix form as $z=TX$, where T is an 8x8 matrix, that have its elements equal to the cosine functions defined before; $x=\{x_0, \dots, x_7\}$ is a row matrix, and z is a column matrix.

$$z_{il} = \frac{c(k)}{2} \sum_{j=0}^7 x_{ij} \cos\left(\frac{(2j+1)l\pi}{16}\right) \tag{2.4}$$

The result of the 1-D DCT on x_{ij} rows. The previous equations suppose that the 2-D DCT can be obtained by performing the 1-D DCT on x_{ij} rows, then performing the 1-D DCT on z_{il} columns. As matrix notation, $Y=TX$ can be seen as $Z=TX'$; $Y=TZ'$. From an implementation point of view, this row-columns computing solution can simplify the hardware necessities, the price being an easy growth of the total number of performed operation.

Compression Method using DWT

This section illustrates the proposed compression technique with pruning proposal based on discrete wavelet transform (DWT). The proposed technique first decomposes an image into coefficients called sub-bands and then the resulting coefficients are compared with a threshold. Coefficients below the threshold are set to zero.

Finally, the coefficients above the threshold value are encoded with a loss less compression technique. The compression features of a given wavelet basis are primarily linked to the relative scarceness of the wavelet domain representation for the signal. The notion behind compression is based on the concept that the regular signal component can be accurately approximated using the following elements: a small number of approximation coefficients (at a suitably chosen level) and some of the detail coefficients. Fig. shows the structure of the wavelet transform based compression.

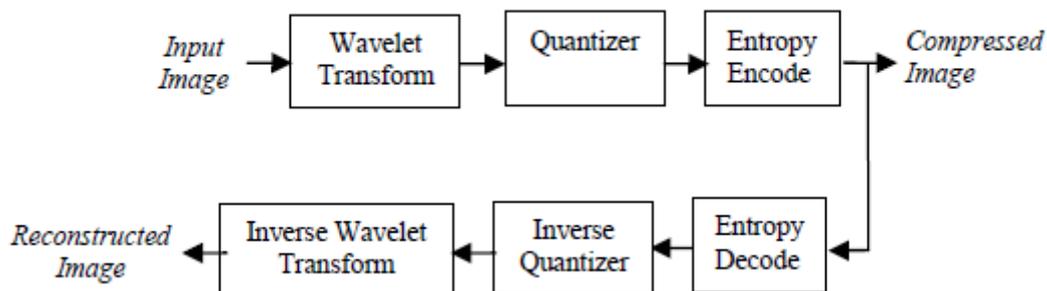


Fig 1 The structure of the wavelet transform based compression

The steps of the proposed compression algorithm based on DWT are described below

1. Decompose

Choose a wavelet; choose a level N. Compute the wavelet. Decompose the signals at level N.

2. Threshold detail coefficients

For each level from 1 to N, a threshold is selected and hard thresholding is applied to the detail coefficients.

3. Reconstruct

Compute wavelet reconstruction using the original approximation coefficients of level N and the modified detail coefficients of levels from 1 to N.

III. PROPOSED ALGORITHM

SUB-BAND IMAGE CODING

In subband coding the input image is filtered through a set of operations that divide the input into a number of bands. The result is a number of sub-images with specific properties; for example, a smoothed version of the original, plus a set of images with the horizontal, vertical, and diagonal edges that are missing from the smoothed version. These sub-images can be compressed more efficiently than the original image, because the restricted type of information in each sub-image allows well-tailored encoding. Advantages over other compression methods include the lack of blocking artifacts, and the flexibility this scheme offers for adaptive compression. The most successful subband coding method is the wavelet decomposition.

A signal is passed through a series of filters to calculate DWT. Procedure starts by passing this signal sequence through a half band digital low pass filter with impulse response $h(n)$. Filtering of a signal is numerically equal to convolution of the tile signal with impulse response of the filter.

$$x[n]*h[n]=\sum_{k=-\infty}^{\infty} x[k].h[n-k] \tag{3.1}$$

A half band low pass filter removes all frequencies that are above half of the highest frequency in the tile signal. Then the signal is passed through high pass filter. The two filters are related to each other as $h[L-1-n]=(-1)^ng(n)$

Filters satisfying this condition are known as quadrature mirror filters. After filtering half of the samples can be eliminated since the signal now has the highest frequency as half of the original frequency. The signal can therefore be subsampled by 2, simply by discarding every other sample. This constitutes 1 level of decomposition and can mathematically be expressed as

$$Y1[n]=\sum_{k=-\infty}^{\infty} x[k]h[2n-k] \tag{3.2}$$

$$Y2[n]=\sum_{k=-\infty}^{\infty} x[k]g[2n+1-k] \tag{3.3}$$

where $y1[n]$ and $y2[n]$ are the outputs of low pass and high pass filters, respectively after subsampling by 2.

This decomposition halves the time resolution since only half the number of sample now characterizes the whole signal. Frequency resolution has doubled because each output has half the frequency band of the input. This process is called as sub band coding. It can be repeated further to increase the frequency resolution as shown by the filter bank.

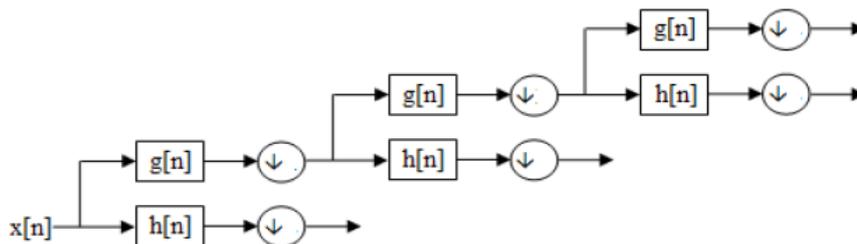


Fig: 2 Filter bank

IV. RESULTS AND DISCUSSIONS

Image compression provides sufficient high compression ratios with no appreciable degradation of image quality. The effectiveness and robustness of this approach has been justified using a set of real images.



Fig 3 original and DCT compression image

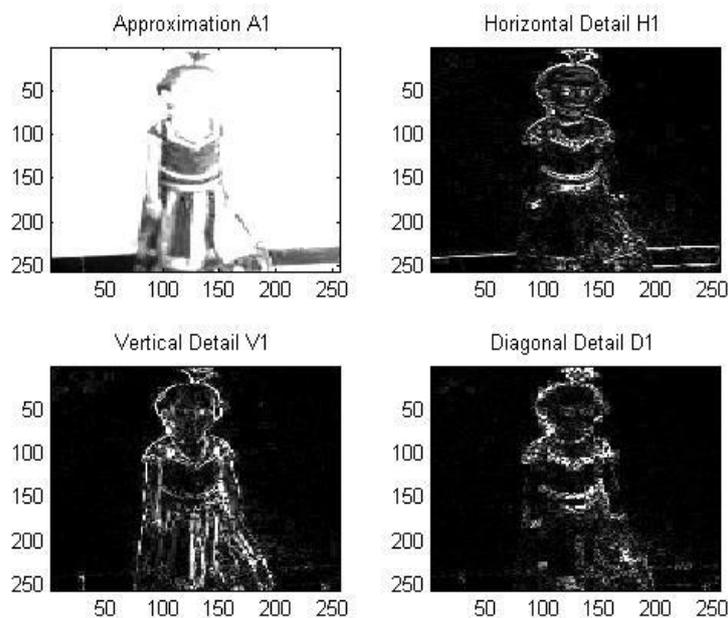


Fig 4 subband compression images



DCT image

Subband image

Fig 5 out images of DCT and subband coding

	Compression Ratio	PSNR
Haar	99.5733%	-34.59
DCT	50%	-42.07

V. CONCLUSIONS

The proposed technique is aimed at developing computationally efficient and effective algorithm for lossy image compression using wavelet techniques. From above observations it is realized that compression ratio and PSNR got by DWT is more than that of DCT. Greater PSNR gives better picture quality

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